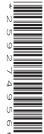


Cambridge Assessment International Education

Cambridge Ordinary Level

CANDIDATE NAME					
CENTRE NUMBER			ANDIDATE JMBER		



STATISTICS 4040/22

Paper 2 October/November 2019

2 hours 15 minutes

Candidates answer on the Question Paper.

Additional Materials: Pair of compasses

Protractor

Electronic calculator

READ THESE INSTRUCTIONS FIRST

Write your centre number, candidate number and name in the spaces at the top of this page.

Write in dark blue or black pen.

You may use an HB pencil for any diagrams or graphs.

Do not use staples, paper clips, glue or correction fluid.

DO NOT WRITE IN ANY BARCODES.

Answer all questions.

If working is needed for any question it must be shown below that question.

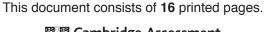
Essential working must be shown for full marks to be awarded.

Electronic calculators should be used.

At the end of the examination, fasten all your work securely together.

The number of marks is given in brackets [] at the end of each question or part question.

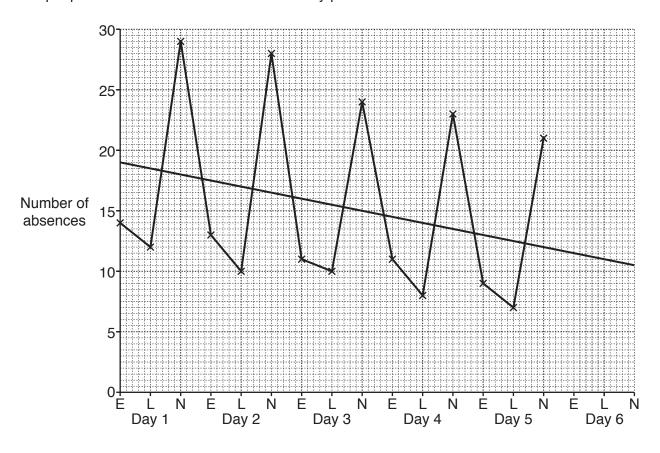
The total number of marks for this paper is 100.





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1 Each employee at a factory works one of three possible shifts, either an Early (E) or a Late (L) or a Night (N) shift each day. The time series graph and trend line give information about the number of people absent for each shift over a five-day period.



The factory owner has been trying to reduce the number of people who are absent.

(a)	Use the graph above to decide whether or not you think he has been successful over the five days. Give a reason for your answer.	∍se
		[1]

(b) Use the time series graph and trend line to find an estimate for the seasonal component of the Late (L) shift.

[2]
 [ပ]

(c) Use the graph and your answer to part (b) to estimate the number of people who will be absent on the Late (L) shift of day 6.

[2		. [2]
----	--	-------

2

An inspector at a bus company wishes to conduct mechanical tests on a sample of the 40 buse parked at the bus station overnight. He numbers the buses from 00 to 39.) buses											
(a)					numb f size		ble b	elow	, star	ting a	at the	e beg	innin	g of	the ta	able,	to se	elect a	simple
	52	31	01	24	00	12	79	27	31	11	36	83	68	80	35	98	16	27	
																			[2]
			•		ered (e bus		17) a	are si	mall I	ocal	buse	s and	d 22 (of the	buse	es (n	umbe	ered 1	8 to 39)
(b)	Cor of b		nt on	whe	ther	or no	t you	ır saı	mple	is re	prese	entati	ive ir	tern	ns of	the t	wo d	ifferer	nt types
																			[3]

3 The students at a school compete in the high jump and the long jump, recording their best result for each event. The table below gives information about the recorded results and scaled results for two of the students, Makena and Ebele, together with the means and standard deviations for the whole school.

	Recorded	results (m)	Scaled results (m)			
	High jump	Long jump	High jump	Long jump		
Makena	1.72	5.16	68	58		
Ebele	1.65	4.95	Z	44		
Mean	Х	5.04	50	50		
Standard deviation	0.06	у	12	12		

(a) Find the values of x, y and z.

	<i>x</i> =
	<i>y</i> =
	$z = \dots $ [6]
(b)	Explain why it is useful to calculate scaled results for these events.
	[1]

4	A speed camera on a rural road records, to the nearest km/h, the speeds of the vehicles that
	pass it. Shown below are the recorded speeds of the first 16 vehicles, in order, as they pass it one
	day.

54 60 63 26 26 29 28 32 35 34 53 54 59 61 63 58

(a) Display the data using a stem-and-leaf diagram.

		[4]
(b)	State the maximum possible range of the speeds of these vehicles.	
		F41
		[1]
(c)	Suggest a possible explanation for the shape of the distribution of the data.	
		[1]
(d)	Alternatively the data could have been displayed using a histogram with class widths $10\mathrm{km/h}.$	of
	State an advantage that the stem-and-leaf diagram has over a histogram.	
		[4]

5	A aı	nd <i>B</i> are two events such	that			
			P(A) = 0.75	and	P(B) = 0.6	
	(a)	Show that A and B cann	not be mutually	exclusi	ve events.	
	It ic	also known that $P(A \cup A)$	↓ <i>R</i>) = 0.85			[1]
		Find $P(A \cap B)$.) = 0.03 .			
	(D)	Tilld F (A F 1 B).				
	(c)	Show whether or not A	and <i>B</i> are indep	oenden [.]	t events.	 [2]
	(d)	Find the probability that	either event A	or even	nt <i>B</i> , but not	[2]
						 [1]

......[1]

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(e) Find the probability that neither event A nor event B occurs.

On 1 January 2016 the ages, measured in completed years, of the 60 workers at a company were collected and are summarised in the table below. 6

Age	Frequency	
18–24	12	
25–29	23	
30–39	18	
40–59	7	

	18–24	12		
	25–29	23		
	30–39	18		
	40–59	7		
(a)	Show that	the mid-point	of the 18–24 class is 21.5 .	
			[:	1]
(b)	Calculate 1 January		the mean and the standard deviation of the ages of the workers o	
			Mean =	
			Standard deviation =[6	
On	1 January 2	2018 the same	60 workers were still employed at the company.	
(c)	Find estir 1 January		mean and standard deviation of the ages of the workers of	n

Mean =

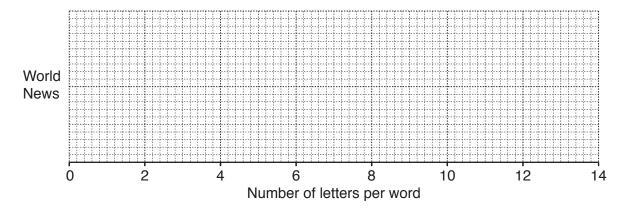
7	An article from the World News section of a newspaper is analysed by counting the number letters in each word of the article. Abbreviations are considered to be single words.	of
	(a) Use statistical language to describe fully the type of data that is being collected.	
		[2]
	The article contains 102 words and has a mean of 4.5 letters per word. The article must be edited so that it contains exactly 100 words. In order to do this, the edireplaces the 3 words 'World Health Organisation' with the abbreviation 'WHO'.	tor
	(b) Find the new mean number of letters per word.	
		[5]
	The table below gives some information about the number of letters per word in the final edit	ed

The table below gives some information about the number of letters per word in the final edited article.

(c) Complete the table.

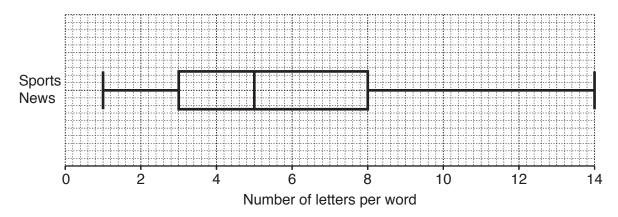
	Number of letters per word
Smallest	1
Largest	
Mean	
Median	4
Lower quartile	
Upper quartile	6.5
Interquartile range	3.5
Standard deviation	2.3
Range	12

(d) Use appropriate information from the table to draw a box-and-whisker diagram for the number of letters per word in the World News article.



[3]

A 100-word article from the Sports News section of the newspaper is also analysed and the box-and-whisker diagram is shown below.



(e)	Make two comparisons between the number of letters per word in the World News article and
	the number of letters per word in the Sports News article.

[2]

8

	ivides a student's cos below is 2016.	of living into five	e categories. The	base year for the p	orice relati
			Price I	relative	
	Category	Weight	2017	2018	
	Housing	35	103	105	
	Food	20	100	102	
	Transport	3		111	
	Clothing	2		98	
	Entertainment	12		115	
Fine	I the price relative of I	lousing in 2018		ne base year. Shov	
	lain what the value of	100 in the table	tells you.		

(e)	(i)	Calculate, correct to one decimal place, a weighted aggregate cost of living index for 2018, taking 2016 as the base year.
		[3]
	(ii)	Explain what this figure suggests.
		[2]
	(iii)	Explain why it would be inappropriate to use this figure for all the people in the country where Amare lives.
		[1]
Am	are s	pent a total of \$6300 in 2016.
(f)	Esti	mate, correct to 3 significant figures, his expenditure in 2018.
		[2]

9 A ranger in a nature reserve counts the geese that she can see and displays her results in a two-way table.

	With tag	Without tag
Barnacle geese	25	14
Pink-footed geese	17	19
Canada geese	10	5

		Pink-footed geese	17	19		
		Canada geese	10	5		
A g	oose is to	be selected at random	1.			
Find	d the prob	ability that				
(a)	it is a pin	ık-footed goose withou	t a tag,			
						[2]
(b)	it has a t	ag,				
						[1]
(c)	it is a ba	rnacle goose, given th	at it has a tag.			
						[1]
Two	geese ar	re to be selected witho	ut replacement.			
(d)	Find the	probability that one is	a barnacle goose and	the other is a pink-foo	ted goose.	

.....[3]

Barnacle geese lay their eggs in nests high up in cliffs away from predators. Young barnacle geese (goslings), unable to fly, jump from these nests to the beach below when they are a few days old. An island of Greenland, with east cliffs and west cliffs, has many such nests. The probabilities of goslings surviving the jump are shown in the table.

Location of nest	Probability of surviving	
East cliffs	0.86	
West cliffs	0.72	

	goslings then try to reach the sea without being caught by arctic foxes. those that survive the jump there is a probability of 0.1 that they will not reach the sea.
(e)	Show that the probability of a gosling from a nest in the east cliffs reaching the sea is 0.774 .
	[2]
	ne particular year there are 83 goslings in nests in the east cliffs and 57 goslings in nests in west cliffs.
(f)	Find the expected number of goslings to reach the sea from these cliffs in that year.
	[3]
	nother year there were twice as many goslings in nests in the east cliffs as in nests in the west s and 79 goslings reached the sea.
(g)	Calculate an estimate for the total number of goslings in nests that year.
	[4]

10 Hazel travels to work by train. She takes a train that departs at the same time each day. On each of 50 mornings she records how late her train arrives at her destination station using the tally chart below.

Number of minutes late, x	Tally	Frequency
0 ≤ <i>x</i> < 8	W W W W	20
8 ≤ <i>x</i> < 16	JHL JHL JHL	15
16 ≤ <i>x</i> < 24	JHL JHL	10
24 ≤ <i>x</i> < 32	IIII	4
32 ≤ <i>x</i> < 40	I	1

From the station she has a 5-minute walk to work and must arrive by 8 am. She is late for work on 11 of these days.

(a)	Use linear interpolation to calculate an estimate, to the nearest minute, for the time that the
	train arrives at her destination station when it is on time.

[.	5]
Hazel complains to the train company about the delays to her train. She decides to quote the largest measure of central tendency in her complaint.	ıе
(b) State which measure of central tendency she should quote. Justify your answer, wire reference to the data in the table.	th

The train company offers to refund her money, as shown in the table below.

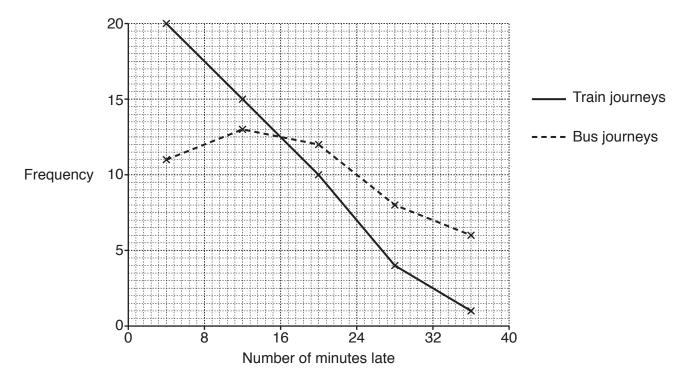
Number of minutes late	Amount of money refunded
Less than 15	Nothing
From 15 to under 30	50% of the cost of the journey
30 or more	100% of the cost of the journey

(c)	Hazel paid \$14.60 for each journey. Use linear interpolation to calculate an estimate for the
	total amount of money she can get back in refunds due to delays to these 50 journeys.

																							٠,	_	
														 									K	0	,

[Question 10 continues on the next page]

For the next 50 days she travels to work by bus and records how late her bus arrives at its destination. Her results for the train journeys and the bus journeys are shown in the frequency polygons below.



(d) State the number of days that her bus was less than 16 minutes late.

	[1]
(e)	Use the frequency polygons to compare the number of minutes late for the train journeys with the number of minutes late for the bus journeys.
	[1]

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