

Cambridge International Examinations Cambridge International General Certificate of Secondary Education

#### CAMBRIDGE INTERNATIONAL MATHEMATICS

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Paper 4 (Extended) MARK SCHEME Maximum Mark: 120

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## MARK SCHEME NOTES

The following notes are intended to aid interpretation of mark schemes in general, but individual mark schemes may include marks awarded for specific reasons outside the scope of these notes.

### **Types of mark**

- M Method marks, awarded for a valid method applied to the problem.
- A Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. For accuracy marks to be given, the associated Method mark must be earned or implied.
- B Mark for a correct result or statement independent of Method marks.

When a part of a question has two or more 'method' steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. The notation '**dep**' is used to indicate that a particular M or B mark is dependent on an earlier mark in the scheme.

#### Abbreviations

answers which round to awrt correct answer only cao dep dependent follow through after error FT ignore subsequent working isw not from wrong working nfww or equivalent oe rounded or truncated rot Special Case SC seen or implied soi

| Question  | Answer  | Marks | Partial Marks  |
|-----------|---|-------|--|
| 1(a)      | 1598 final answer   | 3     | M2 for (23970 × 0.8) ÷ 12 oe<br>or M1 for 23970 × 0.2 or better<br>or for 23970 ÷ 12   |
| 1(b)(i)   | 23 500 nfww   | 3     | <b>M2</b> for 23 970 ÷ 1.02 oe<br>or <b>M1</b> for 23 970 = 102%   |
| 1(b)(ii)  | 2024 nfww   | 3     | M2 for $\frac{\log\left(\frac{30000}{23970}\right)}{\log 1.03}$ oe soi by 7.59or sketch<br>leading to 7.59<br>or 2 trials, one giving 7 and one giving 8<br>or M1 for $23970 \times \left(1 + \frac{3}{100}\right)^n$ [= 30 000] oe seen<br>or reasonable sketch<br>or 3 trials of $23970 \times 1.03^n$<br>or 1 trial giving 8. |
| 2(a)(i)   | Reflection, $y = x$   | 1     |  |
| 2(a)(ii)  | Enlargement [with centre] (2, 1)<br>[scale factor] $\frac{1}{4}$ oe | 2     | B1 for each  |
| 2(a)(iii) | Translation $ \begin{pmatrix} 3 \\ -5 \end{pmatrix} $               | 2     | B1 for each  |
| 2(b)(i)   | Correct triangle<br>(0, 0), (0, 2), (-2, 3)                         | 2     | <b>SC1</b> for rotation 90° clockwise about (0, 0) or rotation 90° anti-clockwise about different centre   |
| 2(b)(ii)  | Correct triangle<br>(0, 0), (4, 0), (6, 2)                          | 2     | SC1 for stretch with s.f. = 2, x-axis invariant or stretch with y-axis invariant with different scale factor.  |
| 3(a)      | 6 points correct  | 3     | <b>B2</b> for 4 or 5 correct<br>or <b>B1</b> for 2 or 3 correct  |
| 3(b)      | Positive  | 1     |  |
| 3(c)(i)   | y = 0.787x + 0.356 final answer                                     | 2     | 0.7874 to 0.7875, 0.3555 to 0.3556<br>B1 for one correct<br>or for $y = 0.79x + 0.36$ final answer   |
| 3(c)(ii)  | 5.4[0]  | 1     | <b>FT</b> from <i>their</i> (c)(i)   |

| Question  | Answer   | Marks | Partial Marks   |
|-----------|--|-------|---|
| 4(a)(i)   | $\begin{pmatrix} -1.5\\1 \end{pmatrix}$ oe         | 1     |   |
| 4(a)(ii)  | $\begin{pmatrix} 10\\ -1 \end{pmatrix}$            | 2     | B1 for each   |
| 4(a)(iii) | $\sqrt{13}$ final answer                           | 2     | <b>M1</b> for $(-3)^2 + 2^2$ oe soi by 3.61 or 3.605 to 3.606 $\sqrt{13}$ in working implies M1   |
| 4(b)      | Correct <i>B</i> clearly indicated                 | 2     | <b>B1</b> for vector $\begin{pmatrix} 1 \\ 5 \end{pmatrix}$ drawn not from <i>A</i> or $\begin{pmatrix} 1 \\ 5 \end{pmatrix}$ seen<br>or correctly following through, from <i>A</i> , their<br>incorrect vector seen.<br>or either $\begin{pmatrix} -3 \\ 2 \end{pmatrix}$ or $\begin{pmatrix} 4 \\ 3 \end{pmatrix}$ correctly drawn <b>only</b> if one<br>starts from <i>A</i> . |
| 5(a)      | 2500   | 2     | <b>M1</b> for 119050 ÷ 47.62  |
| 5(b)(i)   | [0]610 or 610 am oe                                | 2     | <b>B1</b> for [0]025 or [0]340 or 28 h 130 min oe seen  |
| 5(b)(ii)  | 722 or 721.7                                       | 3     | M1 for 4150 ÷ <i>their</i> 5h 45 min<br>B1 for 5.75 oe  |
| 5(b)(iii) | 5 h 32 (or 31.8 to 32[.0]) min                     | 3     | M1 for 4150 ÷ 750 soi by 5.53 or 5.53<br>B1FT for correct conversion to hours and minutes   |
| 6(a)(i)   | [ <i>x</i> =] <i>cv</i> oe                         | 1     |   |
| 6(a)(ii)  | $[y =] kv^2$ oe                                    | 1     |   |
| 6(a)(iii) | $[d =] cv + kv^2 \text{ or } v(c + kv) \text{ oe}$ | 1     | FT  |
| 6(b)(i)   | $750 = 12c + 12^2 k$ oe                            | M1    | isw any cancelling  |
| 6(b)(ii)  | $2050 = 20c + 20^2 k$ oe                           | 1     | isw any cancelling  |
| 6(c)      | [c =] 2.5 oe cao<br>[k =] 5 cao                    | 3     | <ul> <li>M1 for correctly eliminating one variable from <i>their</i> equations in this part. or sketches of lines</li> <li>A1 for either solution If zero scored SC1 for <i>their</i> values satisfying one equation.</li> </ul>  |
| 6(d)      | 8100   | 2     | M1 for correct substitution of 40 into <i>their</i> (a)(iii) containing <i>their</i> values of $c$ and $k$ .  |

| Question | Answer  | Marks | Partial Marks   |
|----------|---|-------|---|
| 7(a)     | Correct sketch showing bearings<br>and distances            | 3     | <ul> <li>B1 for 310° bearing approx correct (270 to 360) and marked</li> <li>B1 for 250° bearing approx correct (180 to 270) and marked</li> <li>B1 for distances correctly marked</li> </ul>   |
| 7(b)     | 120   | 1     |   |
| 7(c)     | $40^2 + 65^2 - 2 \times 40 \times 65 \times \cos$ their 120 | M1    | <i>their</i> 120 must be between 0 and 180<br>Allow $\cos 120 = \frac{40^2 + 65^2 - []^2}{2 \times 40 \times 65}$   |
|          | 91.78 to 91.79  | A2    | <b>A1</b> for 8425 or $5\sqrt{337}$   |
| 7(d)     | 288 or 287.8  | 4     | <b>M2</b> for $\frac{40\sin(their120)}{91.8}$ oe  |
|          |   |       | or M1 for $\frac{\sin \theta}{40} = \frac{\sin(their 120)}{91.8}$ oe<br>If cosine rule used, M2 for explicit expression or<br>M1 for implicit.  |
|          |   |       | A1 for 22.2 or 22.16 to 22.17   |
|          |   |       | If 0 scored <b>SC2</b> for answer 108 or 107.8  |
| 8(a)     | Correct sketch  | 3     | With correct shape with two max on right of <i>y</i> -axis<br>and one on left, all above <i>x</i> -axis and reasonable<br>quality<br>or <b>B2</b> for correct shape and all above <i>x</i> -axis<br>or <b>B1</b> for correct shape            |
| 8(b)     | -270, 90, 450   | 3     | B1 for each<br>SC2 for all correct but with y co-ords<br>or SC1 for two correct with y co-ords  |
| 8(c)     | 750, 870  | 2     | B1 for each   |
| 8(d)     | <i>x</i> < 54.7   | 1     | 54.74 to 54.75  |
|          | 164 < <i>x</i> < 267  | 2     | 163.5 to 163.6, 266.6<br><b>B1</b> for one inequality<br>or <b>B1</b> for both values seen<br>If 0 scored, <b>B1</b> for straight line with negative<br>gradient crossing curve three times between<br>x = 0 and $x = 400$ . May be freehand. |

| Question  | Answer   | Marks | Partial Marks   |
|-----------|--|-------|---|
| 9(a)(i)   | $\frac{1}{2} \times x \times (x+2) \times \frac{\sqrt{3}}{2} \text{ oe or better}$<br>final answer | 2     | <b>M1</b> for $\frac{1}{2} \times x \times (x+2) \times \sin 60$  |
| 9(a)(ii)  | equating to $18\sqrt{3}$ and correct elimination of $\sqrt{3}$                                     | M1    | Dependent on correct answer used from (a)(i)<br>or answer to (a)(i) contains sin60 but is<br>otherwise correct.   |
|           | Completion with at least one step  | A1    | No errors or omissions  |
| 9(b)(i)   | 7.54 or 7.544 , –9.54 or –9.544  | 2     | <b>B1</b> for each<br>If 0 scored, <b>M1</b> for substitution in formula or sketch<br>or $(x + 1)^2 - 73$ or better   |
| 9(b)(ii)  | 6.53 or 6.54 or 6.529 to 6.536   | 2     | M1 for sin $60 = \frac{[]}{their 7.54}$ oe  |
| 10(a)(i)  | $[y=] \frac{1}{2}x+1$  | 3     | <b>M1</b> for gradient = $\frac{8-2}{14-2}$ oe  |
|           |  |       | <b>M1</b> for correct substitution of (2, 2) or (14, 8) into<br>y = (their m)x + c oe soi   |
| 10(a)(ii) | [y=]-2x+26   | 3     | M1 for gradient = $\frac{-1}{their \frac{1}{2}}$  |
|           |  |       | M I for substituting (11, 4) into<br>y = (their - 2)x + c oe soi  |
| 10(b)     | Correct substitution and completion $af(10, 6)$ for both lines as                                  | 2     | <b>B1</b> for either  |
|           |  |       | OR  |
|           |  |       | M1 for correct elimination of <i>x</i> or <i>y</i> from equations A1 for completion to solution (10, 6)   |
| 10(c)     | (9, 8)   | 1     |   |
| 10(d)     | 30 cao   | 4     | <b>M3</b> for $\left[\frac{1}{2}\right] \times \sqrt{12^2 + 6^2} \times \sqrt{2^2 + 4^2}$ oe  |
|           |  |       | or <b>B2</b> for two of $\sqrt{12^2 + 6^2}$ oe ( <i>AC</i> ), $\sqrt{2^2 + 4^2}$ oe   |
|           |  |       | ( <i>BD</i> or <i>MC</i> ), $\sqrt{8^2 + 4^2}$ oe ( <i>AM</i> ), $\sqrt{2^2 + 1^2}$ oe ( <i>MD</i> or <i>MP</i> )   |
|           |  |       | or <b>B1</b> for one of these. ( <i>M</i> is the intersection of <i>AC</i> and <i>BD</i> )  |
|           |  |       | OR  |
|           |  |       | <b>M3</b> for full area e.g. $[0.5 \times 12 \times 6 - 0.5 \times 6 \times 7] \times 2$<br>or <b>B2</b> for 2 correct areas evaluated<br>or <b>B1</b> for 1 correct area evaluated |

| Question  | Answer  | Marks          | Partial Marks   |
|-----------|---|----------------|---|
| 11(a)     | 12.9 or 12.86 to 12.87  | 2              | <b>M1</b> for evidence of at least three mid-interval values 9.5, 11, 13, 15.5 soi by 95, 550, 845, 697.5 or 2187.5   |
| 11(b)     | Correct Histogram   | 4              | B1 for correct bar widths no gaps   |
|           |   |                | <b>B3</b> for 4 correct heights and corresponding scale<br>from 0<br>or <b>B2</b> for 3 correct heights and corresponding scale<br>from 0<br>or <b>B1</b> for 2 correct heights and corresponding scale<br>from 0 |
|           |   |                | or <b>B1</b> for 3 correct frequency densities soi  |
| 11(c)(i)  | $\frac{198}{2873}$ oe   | 2              | <b>M1</b> for $\frac{45}{170} \times \frac{44}{169}$  |
| 11(c)(ii) | $\frac{100}{2873}$ oe   | 3              | <b>M2</b> for $\frac{10}{170} \times \frac{50}{169} + \frac{50}{170} \times \frac{10}{169}$ oe<br>or <b>M1</b> for $\frac{10}{170} \times \frac{50}{169}$   |
| 12(a)     | 11  | 1              |   |
| 12(b)     | 6   | 2              | <b>B1</b> for $h(2) = 1$ soi or $4(x^2 - 3) + 2$ or better  |
| 12(c)     | -3  | 2              | <b>M1</b> for $4x = -10 - 2$  |
| 12(d)     | $h(x) \ge -3$   | 1              | Allow $y \ge -3$  |
| 12(e)     | $\frac{x-2}{4}$ of final answer                                   | 2              | <b>M1</b> for $y - 2 = 4x$ or $x = 4y + 2$ or $\frac{y}{4} = x + \frac{2}{4}$   |
| 12(f)     | Stretch<br>x-axis invariant<br>[Scale factor] 2<br>OR             | 3              | B1 for each   |
|           | Reflection<br>y = -2.70 + 6.75                                    | M1<br>A2       |   |
|           | OR  |                |   |
|           | Rotation<br>(2.5, 0)<br>167 (167.47) or 12.5 (12.53)<br>clockwise | M1<br>A1<br>A1 |   |
| 12(g)     | $[y=] \overline{x^2 - 4x + 1}$                                    | 3              | <b>M2</b> for $y = (x - 2)^2 - 3$<br>or <b>M1</b> for $x - 2$ seen in a quadratic<br>If 0 scored, <b>SC1</b> for $y = x^2 + 4x + 1$   |