



# Cambridge IGCSE™

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**CAMBRIDGE INTERNATIONAL MATHEMATICS**

**0607/51**

Paper 5 (Core)

**May/June 2023**

MARK SCHEME

Maximum Mark: 36

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**Published**

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

Cambridge International will not enter into discussions about these mark schemes.

Cambridge International is publishing the mark schemes for the May/June 2023 series for most Cambridge IGCSE, Cambridge International A and AS Level and Cambridge Pre-U components, and some Cambridge O Level components.

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This document consists of **5** printed pages.

**Generic Marking Principles**

These general marking principles must be applied by all examiners when marking candidate answers. They should be applied alongside the specific content of the mark scheme or generic level descriptors for a question. Each question paper and mark scheme will also comply with these marking principles.

**GENERIC MARKING PRINCIPLE 1:**

Marks must be awarded in line with:

- the specific content of the mark scheme or the generic level descriptors for the question
- the specific skills defined in the mark scheme or in the generic level descriptors for the question
- the standard of response required by a candidate as exemplified by the standardisation scripts.

**GENERIC MARKING PRINCIPLE 2:**

Marks awarded are always **whole marks** (not half marks, or other fractions).

**GENERIC MARKING PRINCIPLE 3:**

Marks must be awarded **positively**:

- marks are awarded for correct/valid answers, as defined in the mark scheme. However, credit is given for valid answers which go beyond the scope of the syllabus and mark scheme, referring to your Team Leader as appropriate
- marks are awarded when candidates clearly demonstrate what they know and can do
- marks are not deducted for errors
- marks are not deducted for omissions
- answers should only be judged on the quality of spelling, punctuation and grammar when these features are specifically assessed by the question as indicated by the mark scheme. The meaning, however, should be unambiguous.

**GENERIC MARKING PRINCIPLE 4:**

Rules must be applied consistently, e.g. in situations where candidates have not followed instructions or in the application of generic level descriptors.

**GENERIC MARKING PRINCIPLE 5:**

Marks should be awarded using the full range of marks defined in the mark scheme for the question (however; the use of the full mark range may be limited according to the quality of the candidate responses seen).

**GENERIC MARKING PRINCIPLE 6:**

Marks awarded are based solely on the requirements as defined in the mark scheme. Marks should not be awarded with grade thresholds or grade descriptors in mind.

Maths-Specific Marking Principles	
1	Unless a particular method has been specified in the question, full marks may be awarded for any correct method. However, if a calculation is required then no marks will be awarded for a scale drawing.
2	Unless specified in the question, answers may be given as fractions, decimals or in standard form. Ignore superfluous zeros, provided that the degree of accuracy is not affected.
3	Allow alternative conventions for notation if used consistently throughout the paper, e.g. commas being used as decimal points.
4	Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored (isw).
5	Where a candidate has misread a number in the question and used that value consistently throughout, provided that number does not alter the difficulty or the method required, award all marks earned and deduct just 1 mark for the misread.
6	Recovery within working is allowed, e.g. a notation error in the working where the following line of working makes the candidate's intent clear.

## MARK SCHEME NOTES

The following notes are intended to aid interpretation of mark schemes in general, but individual mark schemes may include marks awarded for specific reasons outside the scope of these notes.

### Types of mark

- M Method marks, awarded for a valid method applied to the problem.
- A Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. For accuracy marks to be given, the associated Method mark must be earned or implied.
- B Mark for a correct result or statement independent of Method marks.

When a part of a question has two or more 'method' steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. The notation 'dep' is used to indicate that a particular M or B mark is dependent on an earlier mark in the scheme.

### Abbreviations

awrt	answers which round to
cao	correct answer only
dep	dependent
FT	follow through after error
isw	ignore subsequent working
nfw	not from wrong working
oe	or equivalent
rot	rounded or truncated
SC	Special Case
soi	seen or implied

Question	Answer	Marks	Partial Marks																																												
1	Diagrams showing 2 horizontal (not middle row) and 2 vertical (not final column) and 1 upward diagonal	2	<b>B1</b> for two correct new winning lines																																												
2(a)	4 [+] 4 [+] 2 or $2 \times 4 + 2$ or lines or symbols on grid implying 4 horizontal <b>or</b> 4 vertical <b>and</b> 2 diagonal winning lines	<b>C1</b>																																													
	10	<b>1</b>																																													
2(b)	5 [+] 5 [+] 2 or $2 \times 5 + 2$ or lines or symbols on grid implying 5 horizontal <b>or</b> 5 vertical <b>and</b> 2 diagonal winning lines	<b>C1</b>																																													
	12	<b>1</b>																																													
2(c)	14	<b>1</b>																																													
3(a)	<table border="1" style="margin-left: auto; margin-right: auto;"> <thead> <tr> <th rowspan="2">Size of grid</th> <th colspan="4">Number of winning lines.</th> </tr> <tr> <th>H</th> <th>V</th> <th>D</th> <th>T</th> </tr> </thead> <tbody> <tr> <td>3 by 3</td> <td>3</td> <td>3</td> <td>2</td> <td>8</td> </tr> <tr> <td>4 by 4</td> <td>4</td> <td>4</td> <td>2</td> <td>10</td> </tr> <tr> <td>5 by 5</td> <td>5</td> <td>5</td> <td>2</td> <td>12</td> </tr> <tr> <td>6 by 6</td> <td><b>6</b></td> <td><b>6</b></td> <td><b>2</b></td> <td>14</td> </tr> <tr> <td>7 by 7</td> <td><b>7</b></td> <td><b>7</b></td> <td><b>2</b></td> <td><b>16</b></td> </tr> <tr> <td>...</td> <td>...</td> <td>...</td> <td>...</td> <td>...</td> </tr> <tr> <td>20 by 20</td> <td><b>20</b></td> <td><b>20</b></td> <td><b>2</b></td> <td><b>42</b></td> </tr> </tbody> </table>	Size of grid	Number of winning lines.				H	V	D	T	3 by 3	3	3	2	8	4 by 4	4	4	2	10	5 by 5	5	5	2	12	6 by 6	<b>6</b>	<b>6</b>	<b>2</b>	14	7 by 7	<b>7</b>	<b>7</b>	<b>2</b>	<b>16</b>	...	...	...	...	...	20 by 20	<b>20</b>	<b>20</b>	<b>2</b>	<b>42</b>	<b>3</b>	<b>B1</b> for each correct row: 6 by 6, 7 by 7 and 20 by 20
Size of grid	Number of winning lines.																																														
	H	V	D	T																																											
3 by 3	3	3	2	8																																											
4 by 4	4	4	2	10																																											
5 by 5	5	5	2	12																																											
6 by 6	<b>6</b>	<b>6</b>	<b>2</b>	14																																											
7 by 7	<b>7</b>	<b>7</b>	<b>2</b>	<b>16</b>																																											
...	...	...	...	...																																											
20 by 20	<b>20</b>	<b>20</b>	<b>2</b>	<b>42</b>																																											
3(b)	$2n + 2$	<b>2</b>	<b>B1</b> for $2n + k$																																												
3(c)	The total must be even or 290.5 should be a whole number or	<b>1</b>	<b>FT</b> <i>their</i> $2n + k$																																												
3(d)	$\sqrt{324}$ [=18]	<b>C1</b>																																													
	18 correctly substituted into $2n + 2$	<b>C1</b>	<b>FT</b> <i>their</i> 18 and <i>their</i> $2n + 2$ <i>their</i> 18 must come from attempt to find $n$ from 324																																												
	38	<b>1</b>																																													
4(a)	3 by 3 6 6 8 20	<b>1</b>																																													
	Diagram(s) implying 6 horizontal or 6 vertical winning lines	<b>C1</b>																																													

Question	Answer	Marks	Partial Marks																																							
4(b)	4 by 4 8 8 8 24	1																																								
	Diagram showing exactly 4 diagonals in the same direction	C1																																								
4(c)	<table border="1"> <thead> <tr> <th rowspan="2">Size of grid</th> <th colspan="4">Number of winning lines.</th> </tr> <tr> <th>H</th> <th>V</th> <th>D</th> <th>T</th> </tr> </thead> <tbody> <tr> <td>3 by 3</td> <td>6</td> <td>6</td> <td>8</td> <td>20</td> </tr> <tr> <td>4 by 4</td> <td>8</td> <td>8</td> <td>8</td> <td>24</td> </tr> <tr> <td>5 by 5</td> <td>10</td> <td>10</td> <td>8</td> <td>28</td> </tr> <tr> <td>⋮</td> <td>⋮</td> <td>⋮</td> <td>⋮</td> <td>⋮</td> </tr> <tr> <td><math>n</math> by <math>n</math></td> <td><math>2n</math></td> <td><math>2n</math></td> <td>8</td> <td><math>4n + 8</math></td> </tr> </tbody> </table>	Size of grid	Number of winning lines.				H	V	D	T	3 by 3	6	6	8	20	4 by 4	8	8	8	24	5 by 5	10	10	8	28	⋮	⋮	⋮	⋮	⋮	$n$ by $n$	$2n$	$2n$	8	$4n + 8$	4	<b>B1</b> for 5 by 5 row <b>B1</b> for $2n$ seen twice <b>B1</b> for 8 in final row, D column <b>B1FT</b> for correct sum of <i>their expressions</i> in $n$ and <i>their</i> 8 in final row					
Size of grid	Number of winning lines.																																									
	H	V	D	T																																						
3 by 3	6	6	8	20																																						
4 by 4	8	8	8	24																																						
5 by 5	10	10	8	28																																						
⋮	⋮	⋮	⋮	⋮																																						
$n$ by $n$	$2n$	$2n$	8	$4n + 8$																																						
4(d)	$4n + 8 = 36$	C2	<b>FT</b> <i>their</i> $4n + 8$ <b>C1</b> for <i>their</i> $4n + 8 =$ any other square number $< 50$																																							
	Two correct stages shown in the solution of <i>their</i> equation	C1	<b>FT</b> <i>their</i> equation e.g. Subtracting 8 and division by 4																																							
	7 by 7	1																																								
	<b>Alternative Method</b>																																									
	Extending correct totals to 36	(C2)	C1 total of 36 only seen																																							
	Showing grid sizes or values of $n$ with totals or $4 \times 6 + 8 = 32$ and $4 \times 7 + 8 = 36$	(C1)	<b>FT</b> <i>their</i> table if linear totals <b>FT</b> <i>their</i> $4n + 8$																																							
	7 by 7	(1)																																								
5(a)	<table border="1"> <thead> <tr> <th rowspan="2">Size of grid</th> <th colspan="4">Number of winning lines</th> </tr> <tr> <th>H</th> <th>V</th> <th>D</th> <th>T</th> </tr> </thead> <tbody> <tr> <td>2 by 2</td> <td>2</td> <td>2</td> <td>2</td> <td>6</td> </tr> <tr> <td>2 by 3</td> <td>4</td> <td>3</td> <td>4</td> <td>11</td> </tr> <tr> <td>2 by 4</td> <td>6</td> <td>4</td> <td>6</td> <td>16</td> </tr> <tr> <td>2 by 5</td> <td>8</td> <td>5</td> <td>8</td> <td>21</td> </tr> <tr> <td>⋮</td> <td>⋮</td> <td>⋮</td> <td>⋮</td> <td>⋮</td> </tr> <tr> <td>2 by <math>w</math></td> <td><math>2w - 2</math></td> <td><math>w</math></td> <td><math>2w - 2</math></td> <td><math>5w - 4</math> oe</td> </tr> </tbody> </table>	Size of grid	Number of winning lines				H	V	D	T	2 by 2	2	2	2	6	2 by 3	4	3	4	11	2 by 4	6	4	6	16	2 by 5	8	5	8	21	⋮	⋮	⋮	⋮	⋮	2 by $w$	$2w - 2$	$w$	$2w - 2$	$5w - 4$ oe	4	<b>B1</b> for 2 by 4 row <b>B1</b> for 2 by 5 row  <b>B1</b> for $2w - 2$ oe seen twice <b>B1</b> for correct sum of <i>their expressions</i> in $w$ in final row
	Size of grid		Number of winning lines																																							
H		V	D	T																																						
2 by 2	2	2	2	6																																						
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⋮	⋮	⋮	⋮	⋮																																						
2 by $w$	$2w - 2$	$w$	$2w - 2$	$5w - 4$ oe																																						
	One correct diagram for 2 by 4 or 2 by 5	C1																																								
5(b)	23	3	<b>M1</b> for <i>their</i> $5w - 4 = 111$ <b>M1</b> for first correct step in solution																																							